

## HOMEWORK (LESSON 12.2)

4.

n	0	1	2	3	4
f(n)	0.1	0.3	0.9	2.7	8.1

Common ratio :  $\frac{0.3}{0.1} = 3$

Recursive :  $f(0) = 0.1, f(n) = 3 f(n-1), n > 0$

Explicit :  $f(n) = 0.1(3)^n$

6.

n	1	2	3	4	5
f(n)	1000	100	10	1	0.1

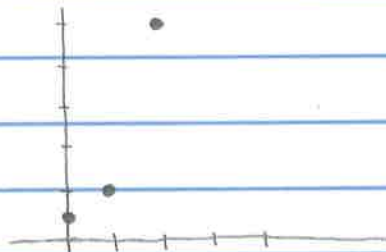
Common ratio :  $\frac{100}{1000} = \frac{1}{10}$

Recursive :  $f(1) = 1000, f(n) = \frac{1}{10} f(n-1), n > 1$

Explicit :  $f(n) = 1000 \left(\frac{1}{10}\right)^{n-1}$

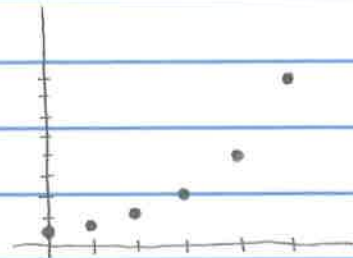
8.  $f(n) = \left(\frac{1}{2}\right) \cdot 4^n, n \geq 0$

n	0	1	2	3	4
f(n)	$\frac{1}{2}$	2	8	32	128



9.  $f(n) = 2 \cdot f(n-1), n \geq 1, f(0) = 0.5$

n	0	1	2	3	4	5
f(n)	$\frac{1}{2}$	1	2	4	8	16



12.

n	0	1	2	3	4
f(n)	1	2	4	8	16

Recursive:  $f(0) = 1, f(n) = 2f(n-1), n > 0$ Explicit:  $f(n) = 1(2)^{n-0}$ 

$$f(n) = 2^n$$

$$f(4) = 2^4$$

$$f(4) = 16 \quad \boxed{16 \text{ teams}}$$

13.

n	0	1	2	3
f(n)	1024	256	64	16

Recursive:  $f(0) = 1024, f(n) = \frac{1}{4}f(n-1), n > 0$ Explicit:  $f(n) = 1024 \left(\frac{1}{4}\right)^n$ 

$$1 = 1024 \left(\frac{1}{4}\right)^n$$

$$\frac{1}{1024} = \left(\frac{1}{4}\right)^n$$

$$4^{-5} = (4^{-1})^n$$

$$-5 = -n$$

$$n = 5 \quad \boxed{5 \text{ games}}$$

14.

Ⓐ.

n	0	1	2	3	4
f(n)	1	2	4	8	16

Recursive:  $f(0) = 1, f(n) = 2f(n-1), n > 0$ Explicit:  $f(n) = 1(2)^n$ 

$$f(6) = 2^6$$

$$f(12) = 2^{12}$$

$$f(6) = 64$$

$$f(12) = 4096$$

$$\boxed{64 \text{ ancestors}}$$

$$\boxed{4096 \text{ ancestors}}$$

Ⓑ.

n	1	2	3	4	5
f(n)	1	2	4	8	16

Explicit:  $f(n) = 1(2)^{n-1}$ 

$$\boxed{f(n) = 2^{n-1}}$$